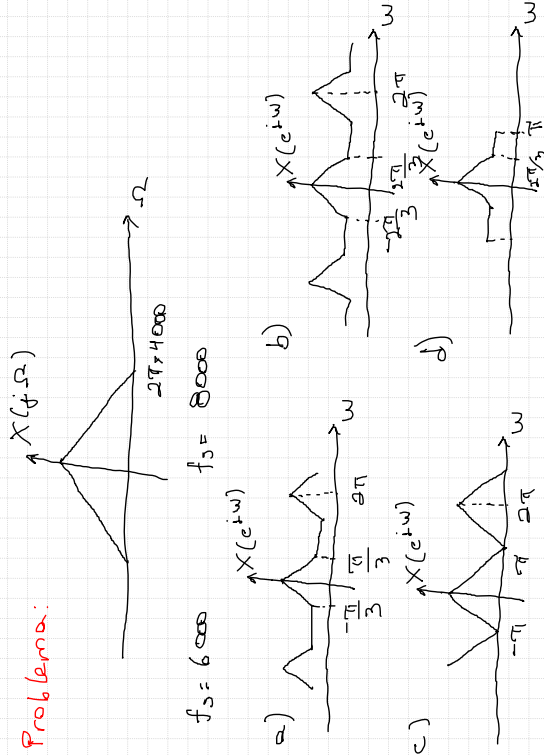


Problema:

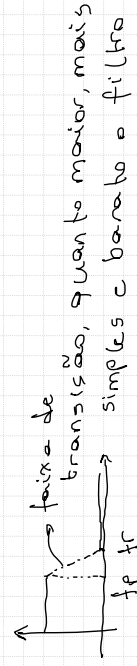


Consequência prática: filtro anti-aliasing

CD: $f_s = 44100$

Maior freq. de interesse: 20000

Especificar freq. passagem e rejeição do filtro passa-baixas colocado antes do ADC



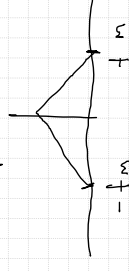
Pq. espectro $X(e^{j\omega})$ é periódico

$x_1[n] = e^{j\omega_1 n}$ e $x_2[n] = e^{j(\omega_1 + 2\pi)n}$
 $= e^{j\omega_1 n} e^{j2\pi n} = e^{j\omega_1 n} = x_1[n]$

Como $x_1[n] = x_2[n]$, componente de um sinal na frequência ω_0 é necessariamente igual à sua componente na freq. $\omega_0 + 2\pi$, pois ambas as freqs. correspondem ao mesmo sinal.

- a) $f_p = 20000$
 $f_r = 22050$
- b) $f_p = 10000$
 $f_r = 22050$
- c) $f_p = 20000$
 $f_r = 44100$
- d) $f_p = 20000$
 $f_r = 24100$
- e) $f_p = 22050$
 $f_r = 44100$

Condição para evitar aliasing:



Separação deve ser menor que $f_s/2$

$2f_m < f_s \Rightarrow f_m < f_s/2$ Taxa de Nyquist

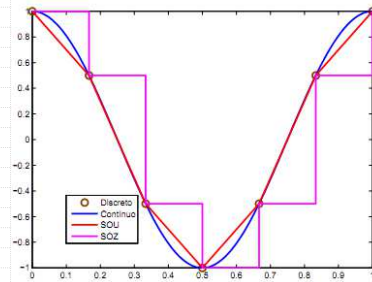
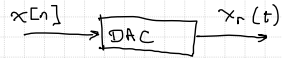
Tem que ser estritamente menor. Exemplo:

$$x(t) = \sin\left(2\pi \frac{1}{2} t\right) \Rightarrow x[n] = \sin(\pi n) = 0$$

No futuro, discutir que $\cos(2\pi f_s/2t + \text{fase})$, não dá para saber se as amostras diferem por amplitude ou pela fase.

Reconstrução

Recado aulas
futura

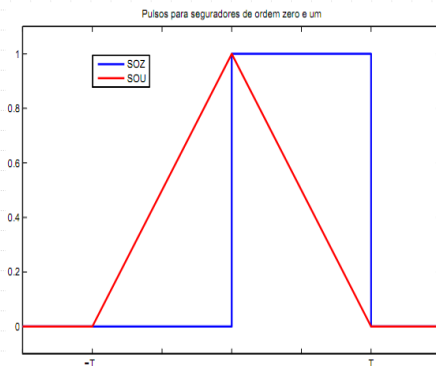


zoom



Como descrever as distorções, as altas frequências que aparecem?

Matematicamente, DAC é caracterizada por um pulso $p(t)$

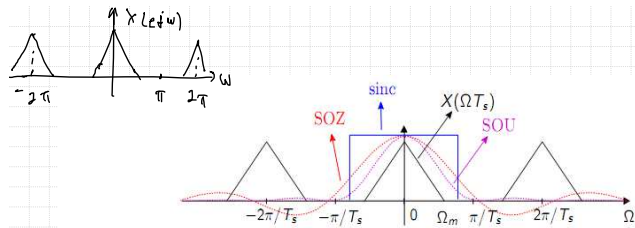
$$x_r(t) = \sum_{n=-\infty}^{\infty} x[n] p(t - nT_s)$$


Em freq,

$$\begin{aligned} X(j\omega) &= \int_{-\infty}^{\infty} x_r(t) e^{-j\omega t} dt \\ &= \sum_{n=-\infty}^{\infty} x[n] \int_{-\infty}^{\infty} p(t - nT_s) e^{-j\omega t} dt \\ &= \sum_{n=-\infty}^{\infty} x[n] e^{-j\omega T_s n} P(j\omega) \\ &= P(j\omega) X(e^{j\omega T_s}) \end{aligned}$$

Handwritten notes in blue ink:

- $\approx \{p(t - nT_s)\}$ (next to the integral)
- $\mathcal{F}\{x[n]\} = X(e^{j\omega T_s})$ (next to the final equation)
- $\sum_{n=-\infty}^{\infty} x[n] e^{j\omega n}$ (below the final equation)



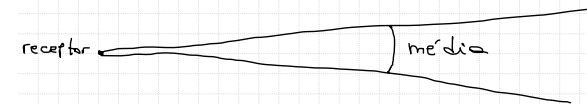
Pulsos práticos

- Distorção na faixa de frequência de interesse.
- Introdução de componentes de alta frequência.

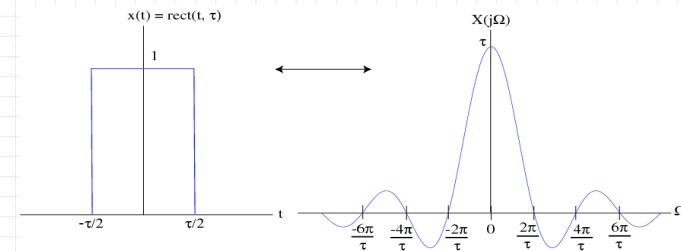
Pulso sinc

- Permite recuperação perfeita do sinal se $\Omega_m < 2\omega_s$.

Voltando ao olho

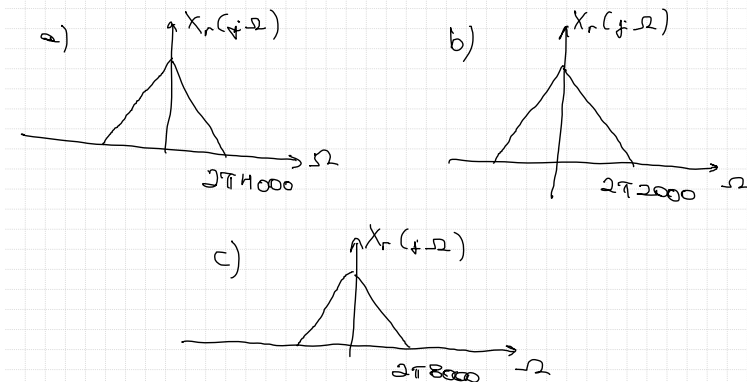
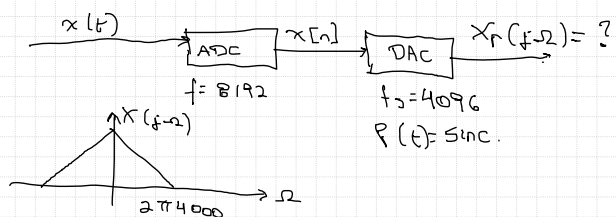


média é filtro passa-baixas. Quanto mais longe, mais longa a média, mais corta altas freqs.



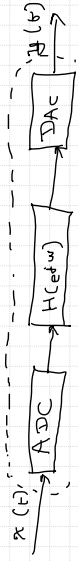
Fonte: <http://cnx.org/content/m32899/1.8/>

Problema:



Problema:

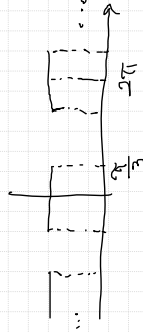
Processamento digital de sinais analógicos:



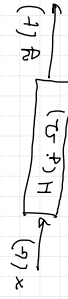
$$H(e^{j\omega})$$

$$f_s = 1000$$

ADC e DAC ideais

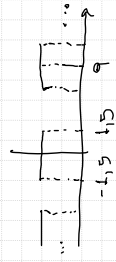


Qual o sistema analógico equivalente?



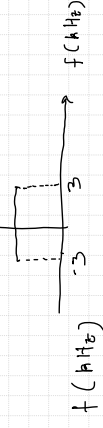
a)

$$H(f)$$



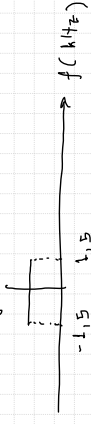
b)

$$H(j\Omega)$$



c)

$$H(f/2)$$



d)

